## Math 2A - Chapter 9 Test - Fall '07 Name:

Show your work for credit. No calculators are needed.

1. Let $\vec{v}=\langle 2,3,6\rangle$. Find two unit vectors parallel to $\vec{v}$.
2. What work is done by the force vector $\vec{F}=\langle 1,2,3\rangle$ in moving an object from the origin to $(2,3,4)$ ? Assume the force is measured in Newtons and the distances are measured in meters.
3. Find the angle between the vectors $\overrightarrow{O P}$ and $\overrightarrow{O Q}$ where the coordinates
are $O 0,0,0 \quad P 2,0,0$, and $Q 2,1,1$.
4. Find the distance between the plane $x-2 y+4 z=0$ and the plane $x-2 y+4 z=7$.
5. Find an equation for the plane $S$ containing the $x$-axis and passing through the point $P(1,2,3)$.
6. Consider the quadric surface described by the equation $2 x^{2}-4 x+y^{2}+z^{2}+4=0$
a. Write the equation in standard form
b. Identify the surface as one of the following: a hyperbolic paraboloid, an elliptical cone, an elliptical paraboloid, an ellipsoid, a hyperboloid of one sheet or a hyperboloid of two sheets.
c. What is the intersection of the surface with the plane $x=2$ ?
7. Find the magnitude of the torque vector at $P$ if a 20 Newton force is applied to the rigid body shown in the diagram at right. Note that this is a planar diagram. Recall that $|\vec{\tau}|=|\vec{r}||\vec{F}| \sin \theta$ where $\vec{r}$ is the lever arm vector $\vec{F}$ is the force vector and $\theta$ is the angle between them.
8. Describe the cross section that the given plane makes with the surface $z=x^{2}-4 y^{2}$
a. $z=9$
b. $x=2 y$

9. The spherical coordinates of a point are $\rho, \theta, \phi=\left(2, \frac{7 \pi}{6},-\frac{\pi}{4}\right)$
a. What are the rectangular coordinates?
b. What are the cylindrical coordinates?
10. Write the equation $x^{2}+y^{2}=4 y$
a. Using cylindrical coordinates.
b. Using spherical coordinates.
