

## Background Theory

Now that you have (it is hoped) developed working code for exploring knight's tours using a human decision-maker, we want to explore further by automating this process using various heuristics and also examine the donut topology.



## 1 Problems

Adapt the knight's tour program to

1. Use the accessibility heuristic of going to the least accessible squares first (choosing randomly in the case of a tie) to automate the search for a knight's tour.

```
int access[8][8] = {{2,3,4,4,4,4,3,2},
                   {3,4,6,6,6,6,4,3},
                   {4,6,8,8,8,8,6,4},
                   {4,6,8,8,8,8,6,4},
                   {4,6,8,8,8,8,6,4},
                   {4,6,8,8,8,8,6,4},
                   {3,4,6,6,6,6,4,3},
                   {2,3,4,4,4,4,3,2}};
```

Allow the user to choose the number of rows and columns of the "chess" board.

Here is some starter code that may or may not be helpful:

```
1
  /// GH working on knights tour 20151015
3
  /**
5   1 14  9 22  3
```

7	18	23	2	15	10						
	13	8	17	4	21						
9	24	19	6	11	16						
	7	12	0	20	5						
11	1	10	21	16	7						
	20	15	8	11	22						
13	9	2	23	6	17						
	14	19	4	0	12						
15	3	24	13	18	5						
17	1	22	3	18	25	30	13	16			
	4	19	24	29	14	17	34	31			
19	23	2	21	26	35	32	15	12			
	20	5	56	49	28	41	36	33			
21	57	50	27	42	61	54	11	40			
	6	43	60	55	48	39	0	37			
23	51	58	45	8	53	62	47	10			
	44	7	52	59	46	9	38	63			
25	1	20	3	16	23	28	33	14	39		
27	4	17	22	27	34	15	38	29	32		
	21	2	19	24	55	36	31	40	13		
29	18	5	76	35	26	41	54	37	30		
	77	62	25	56	75	72	43	12	47		
31	6	57	74	79	42	53	46	71	44		
	63	78	61	52	73	70	67	48	11		
33	58	7	80	65	60	9	50	45	68		
	0	64	59	8	51	66	69	10	49		
35	1	32	3	22	29	48	35	20	39	42	
37	4	23	30	49	34	21	44	41	36	19	
	31	2	33	28	47	62	79	38	43	40	
39	24	5	50	63	78	45	60	89	18	37	
	51	64	27	46	61	90	77	80	59	88	
41	6	25	66	85	70	81	94	87	92	17	
	65	52	69	26	95	86	91	76	99	58	
43	10	7	84	67	82	71	0	93	16	75	
	53	68	9	12	55	96	73	14	57	98	
45	8	11	54	83	72	13	56	97	74	15	
47	1	22	3	28	25	20	57	30	35	18	55
	4	27	24	21	58	29	36	19	56	31	34
49	23	2	61	26	37	74	59	68	33	54	17
	62	5	38	79	60	67	72	75	52	69	32
51	39	80	63	66	73	92	77	70	99	16	53
	6	65	82	91	78	71	98	115	76	51	100
53	81	40	89	64	97	112	93	108	101	114	15
	44	7	96	83	90	107	116	113	120	103	50
55	41	84	43	88	111	94	109	102	117	14	119
	8	45	86	95	10	47	106	0	12	49	104
57	85	42	9	46	87	110	11	48	105	118	13



113	1	34	3	30	37	42	47	28	45	74	89	26	69	72	
115	4	31	36	41	48	29	44	75	94	27	70	73	88	25	
117	35	2	33	38	43	76	95	46	83	90	107	130	71	68	
119	32	5	52	77	40	49	82	93	106	129	84	87	24	131	
121	53	78	39	50	81	96	105	128	91	108	135	132	67	86	
123	6	51	80	97	104	127	92	109	158	133	148	85	136	23	
125	79	54	103	116	99	110	179	126	173	150	159	134	147	66	
127	102	7	98	111	182	125	172	175	180	157	168	149	22	137	
129	55	112	117	100	115	190	181	178	171	174	151	160	65	146	
131	8	101	114	191	124	183	176	185	188	167	156	169	138	21	
133	113	56	123	118	195	186	189	166	177	170	161	152	145	64	
135	12	9	0	121	192	119	184	187	164	155	144	141	20	139	
137	57	122	11	14	59	194	165	16	61	162	153	18	63	142	
139	10	13	58	193	120	15	60	163	154	17	62	143	140	19	
141															
143	1	30	3	36	33	28	85	38	47	26	75	40	45	24	73
145	4	35	32	29	86	37	48	27	84	39	46	25	74	41	44
147	31	2	89	34	49	104	87	114	107	76	83	80	43	72	23
149	90	5	50	103	88	113	108	105	82	145	140	77	70	79	42
151	51	100	91	112	109	102	115	158	139	106	81	146	151	22	71
153	6	93	110	101	116	159	138	123	144	195	154	141	78	69	152
155	99	52	117	92	111	122	161	196	157	142	147	194	153	150	21
157	94	7	98	121	160	137	124	143	198	201	208	155	148	185	68
159	53	118	95	136	125	162	197	176	207	156	199	202	193	20	149
161	8	97	120	127	134	175	168	215	200	209	206	213	186	67	184
163	119	54	135	96	163	126	177	210	217	214	219	192	203	188	19
163	58	9	128	133	174	169	216	167	220	205	212	187	224	183	66

165	55	130	57	164	171	166	173	178	211	218	0	204	191	18	189		
167	10	59	132	129	12	61	170	221	14	63	180	223	16	65	182		
169	131	56	11	60	165	172	13	62	179	222	15	64	181	190	17		
171																	
173	1	32	3	38	35	42	29	40	77	94	27	74	111	70	25	72	
175	4	37	34	43	30	39	78	93	28	75	110	115	26	73	112	69	
177	33	2	31	36	79	92	41	76	109	132	95	120	113	136	71	24	
179	46	5	80	89	44	99	108	131	96	121	114	143	116	119	68	137	
181	81	86	45	100	91	88	97	124	159	144	133	122	135	142	23	118	
183	6	47	90	87	98	125	160	107	130	123	158	141	146	117	138	67	
185	85	82	101	126	161	106	129	164	217	204	145	134	157	140	147	22	
187	48	7	84	105	128	163	216	207	186	165	156	203	148	151	66	139	
189	83	102	127	162	215	208	187	218	235	250	205	166	155	168	21	150	
191	8	49	104	209	188	219	214	249	206	185	234	183	202	149	152	65	
193	103	210	189	220	213	238	225	236	251	248	255	176	167	154	169	20	
195	50	9	212	227	224	231	252	247	0	233	184	201	182	177	64	153	
197	211	190	221	194	239	226	237	232	245	254	243	178	175	170	19	60	
199	10	51	228	223	230	195	246	253	242	179	198	181	200	61	172	63	
201	191	222	53	12	193	240	55	14	197	244	57	16	171	174	59	18	
203	52	11	192	229	54	13	196	241	56	15	180	199	58	17	62	173	
205																	
207	1	36	3	32	39	44	49	30	47	104	123	28	101	138	143	26	99
209	4	33	38	43	50	31	46	105	122	29	102	137	144	27	100	139	142
211	37	2	35	40	45	106	121	48	103	136	145	124	159	154	141	98	25
213	34	5	54	107	42	51	112	135	120	125	176	153	146	165	160	157	140
215	55	108	41	52	111	128	119	126	177	152	147	166	175	158	155	24	97
217	6	53	110	129	118	113	134	151	148	189	174	179	164	167	172	161	156

219	109	56	117	114	133	150	127	190	193	178	183	188	173	180	163	96	23	
221	116	7	132	197	130	209	194	149	204	191	242	181	184	187	168	171	162	
223	57	198	115	208	195	206	203	192	241	182	251	186	255	170	227	22	95	
225	8	213	196	131	210	269	240	205	264	259	254	243	252	185	256	169	226	
227	199	58	211	234	207	202	275	270	267	250	263	260	257	228	245	94	21	
229	212	9	214	201	276	239	268	265	274	279	258	253	244	261	92	225	84	
231	59	200	235	238	233	284	281	278	271	266	249	262	229	246	85	20	93	
233	10	215	66	285	236	277	232	283	280	273	230	247	86	91	224	83	74	
235	63	60	237	218	67	282	287	272	231	248	87	90	223	82	75	78	19	
237	216	11	62	65	286	13	220	69	288	15	222	71	88	17	80	73	76	
239	61	64	217	12	219	68	0	14	221	70	89	16	81	72	77	18	79	
241	1	42	3	38	45	50	55	36	53	102	121	34	99	136	85	32	83	94
243	4	39	44	49	56	37	52	103	120	35	100	135	142	33	98	93	86	31
245	43	2	41	46	51	104	119	54	101	134	143	122	137	92	141	84	95	82
247	40	5	60	105	48	57	110	133	118	123	166	151	144	153	138	97	30	87
249	61	106	47	58	109	126	117	124	167	150	145	162	183	140	91	154	81	96
251	6	59	108	127	116	111	132	149	146	165	182	187	152	161	184	139	88	29
253	107	62	115	112	131	148	125	168	181	188	163	208	185	196	155	90	157	80
255	114	7	130	177	128	169	180	147	164	209	186	195	200	207	160	197	28	89
257	63	176	113	170	179	192	293	210	189	194	265	206	225	198	201	156	79	158
259	8	171	178	129	298	211	190	193	300	275	224	199	264	205	252	159	202	27
261	175	64	297	212	191	292	299	294	223	266	287	276	269	226	263	204	251	78
263	172	9	174	307	296	303	222	319	286	301	274	267	272	279	270	253	26	203
265	65	308	213	304	291	320	295	302	283	288	285	280	277	268	227	262	77	250
267	10	173	310	315	306	221	318	289	322	239	282	273	246	271	278	249	254	25
269	309	66	305	214	317	290	321	220	243	284	245	234	281	248	255	228	261	76

```
271 14 11 316 311 314 215 242 323 240 219 238 247 236 233 260 257 24 229
273 67 312 13 16 69 0 217 18 71 244 235 20 73 256 231 22 75 258
275 12 15 68 313 216 17 70 241 218 19 72 237 232 21 74 259 230 23
**/
277 #include "..\std_lib_facilities.h"
#include <fstream>
279 #include <windows.h> //for colors

281 ///global variable for board width and length
int bWidth{8}, bLength{8};
283 bool debug = false;

285 ///fixed array of possible moves
int movArr[8][2] = {{-1, 2},{-2, 1},{-2,-1},{-1,-2},
287 { 1,-2},{ 2,-1},{ 2, 1},{ 1, 2}};
/*****/
289 ///prototypes
void ClearScreen();
291
void displayBoard(vector <int>);
293
/// choose a legal move and update
295 void getMove(vector<int>& brd,
int& mve,
297 int& currPos,
vector<int>& access,
299 vector<string> poem,
vector<string>& sPoem);
301
///initialize the board and set first position
303 void start(vector<int>&, int&, vector<int>&);

305 ///set up the access matrix
void setup_access(vector<int>&);
307
///check to see if stuck
309 bool stuck(vector<int> brd, int pos);

311 /// get the index of the first accessible square with the lowest accessibility nu
/// searching counter-clockwise from (-1,2)
313 int getMinAccess(vector<int> accBrd, vector<int> brd, int pos);

315 /// update accessibility matrix
void updateAcc(vector<int>& accBrd, int pos);
317
bool donut{false};
319
int main() {
321 string poemName, word;
vector<string> poem, sPoem;
323 cout << "\nEnter the file name for your poem:\n";
```

```
    cin >> poemName;
325 ifstream inFile(poemName);
    int i{0};
327 while(inFile>>word) {
        poem.push_back(word);
329     ++i;
    }
331 sPoem.push_back(poem[0]);
    cout << "\nThere are " << i << " words." << endl;
333 cout << "\nEnter the width and length of your board:";
    cin >> bWidth >> bLength;
335 cout << "\nDo you want to use donut topology?";
    cin >> donut;
337 vector<int> board(bWidth*bLength); // the board of moves
    int mve{1}, currPos{0};
339 if(donut) vector<int> access(bWidth*bLength,8);
    else {
341     vector<int> access(bWidth*bLength); // accessibility board
        setup_access(access);
343     }
    if(debug) {
345     cout << "\nIn doubt about access:" << endl;
        displayBoard(access);
347     cin.get();
    }
349
    //get first position and update accessibility matrix
351 start(board , currPos , access);

    //game loop
353 displayBoard(board);
355 while(!stuck(board, currPos) && mve << bWidth*bLength-1) {
        ClearScreen();
357     getMove(board, currPos, mve, access, poem, sPoem);
        displayBoard(board);
359     //cout << "\n" << sPoem[sPoem.size()-1];
        //cin.get();
361 }

    // print out scrambled poem
363 cout << "\n\nThe scrambled poem is\n\n";
    int j = 0;
    //for(string s: poem) {
367 for(int j = 0; j < sPoem.size(); ++j) {
        cout << sPoem[j] << " ";
369     if((j+1)%10 == 0) cout << endl;
    }
371
    cout << "\n\nHere is the poem unscrambled:\n\n";
373 // to do: write code to unscramble the poem
    return 0;
375 }
```

```
377 ///initialize the board and set first position
void start(vector<int>& brd, int& cp, vector<int>& access) {
379     int row , col;
    cout << "\nWhat row and column position do you want to start?";
381     cin >> row >> col;
    cout << "\nThat's at " << row*bWidth+col << endl;
383     cp = row*bWidth+col;
    brd[cp] = 1;
385     updateAcc(access, cp);
    ///debugging
387     if(debug) displayBoard(access);
}
389
void displayBoard(vector<int> board) {
391     for(int i = 0; i < board.size(); ++i) {
        cout << setw(4) << board[i];
393         if((i+1)%bWidth == 0) cout << "\n\n";
    }
395 }

397 void getMove(vector<int>& brd,
              int& currPos,
399              int& mve,
              vector<int>& access,
401              vector<string> poem,
              vector<string>& sPoem) {
403     /// update current position

405     /// update access vector
    updateAcc(access, currPos);
407     ++mve;
    brd[currPos] = mve;
409

    ///debugging
411     if(debug) displayBoard(access);
}
413

///set up the access matrix
415 void setup_access(vector<int>& a) {
    int cntr{0};
417     ///for each row
    for(int i = 0; i < bLength; ++i) {
419         ///for each column
        for(int j = 0; j < bWidth; ++j) {
421             cntr = 0;
            if(i-1>=0      && j+2<bWidth) cntr++;
423             if(i-2>=0      && j+1<bWidth) cntr++;
            if(i-2>=0      && j-1>=0    ) cntr++;
425             if(i-1>=0      && j-2>=0    ) cntr++;
            if(i+1<bLength && j-2>=0    ) cntr++;
427             if(i+2<bLength && j-1>=0    ) cntr++;
            if(i+2<bLength && j+1<bWidth) cntr++;
429             if(i+1<bLength && j+2<bWidth) cntr++;
        }
    }
}
```

```
        a[i*bWidth+j]=cntr;
431    } /// end for loop
    } /// end for loop
433    ///debugging for check
    for(int i = 0; i < bWidth*bLength; ++i) {
435        cout << a[i];
        if((i+1)%bWidth==0) cout << endl;
437    }
}
439
///check to see if stuck
441 bool stuck(vector<int> brd, int pos) {
    /// write code that will return true if the knight has nowhere to go
443    /// and return false if there is a move possible
}
445
// return the position number (between 0 and bWidth*bLength-1)
447 int getMinAccess(vector<int> accBrd, vector<int> brd, int pos) {
    /// find first legal move
449    if(!donut) {
        /// write code to find the square with min access with rectangle
451        /// and return the index of that square
    }
453    else // donut mode
        ///upper left corner
455    if(pos==0) {
        mmmm = bWidth*(bLength-1) + 2; //22
457        if(accBrd[bWidth*(bLength-2)+1] < accBrd[mmmm])
            mmmm = bWidth*(bLength-2)+1; //16
459        if(accBrd[bWidth*(bLength-1)-1] < bWidth[mmmm])
            mmmm = bWidth*bLength-2; //19
461        if(accBrd[bWidth*bLength-2] < bWidth[mmmm])
            mmmm = bWidth*bLength-2; //23
463        if(accBrd[2*bWidth-2] < bWidth[mmmm])
            mmmm = 2*bWidth-2; //8
465        if(accBrd[3*bWidth-1] < bWidth[mmmm])
            mmmm = 3*bWidth-1; //14
467        if(accBrd[2*bWidth+1] < bWidth[mmmm])
            mmmm = 2*bWidth+1; //11
469        if(accBrd[bWidth+2] < bWidth[mmmm])
            mmmm = bWidth+2; //7
471        return mmmm;
    }
473    ///upper left corner+1
    ///upper right corner
475    ///lower right corner
    ///lower left corner
477    /// and so on, lots of special cases around the corner
}
479
481 /// update accessibility matrix
void updateAcc(vector<int>& access, int currPos) {
```

```
483     /// write code to update access vector
484 }
485
486 void ClearScreen() {
487     HANDLE          hStdOut;
488     CONSOLE_SCREEN_BUFFER_INFO csbi;
489     DWORD           count;
490     DWORD           cellCount;
491     COORD           homeCoords = { 0, 0 };
492
493     hStdOut = GetStdHandle( STD_OUTPUT_HANDLE );
494     if (hStdOut == INVALID_HANDLE_VALUE) return;
495
496     /* Get the number of cells in the current buffer */
497     if (!GetConsoleScreenBufferInfo( hStdOut, &csbi )) return;
498     cellCount = csbi.dwSize.X * csbi.dwSize.Y;
499
500     /* Fill the entire buffer with spaces */
501     if (!FillConsoleOutputCharacter(
502         hStdOut,
503         (TCHAR) ' ',
504         cellCount,
505         homeCoords,
506         &count)) return;
507
508     /* Fill the entire buffer with the current colors and attributes */
509     if (!FillConsoleOutputAttribute(
510         hStdOut,
511         csbi.wAttributes,
512         cellCount,
513         homeCoords,
514         &count)) return;
515
516     /* Move the cursor home */
517     SetConsoleCursorPosition( hStdOut, homeCoords );
518 }
```

2. Allow the user to play on the donut topology so that, initially, on a board which is at least 5 by 5, each square has accessibility number 8.