

Write responses to questions 1 and 2 on this paper or attach additional sheets, as necessary. For all subsequent problems, use separate paper. Do not use a computer.

Assume the necessary libraries are included and appropriate namespaces are used.

1. Match each of the following terms on the left with its definition on the right.

- |                                 |   |
|---------------------------------|---|
| (a) <b>declaration</b> _____    | (1) Something that defines a range of possible values and a set of operations for an object.                            |
| (b) <b>byte</b> _____           | (2) A named unit of code that can be invoked (called) from different parts of a program; a logical unit of computation. |
| (c) <b>narrowing</b> _____      | (3) A declaration that allocates memory and assigns all necessary value(s) for it.                                      |
| (d) <b>invariant</b> _____      | (4) the most basic unit of information in a computer that can have the value 0 or 1.                                    |
| (e) <b>Compile errors</b> _____ | (5) A named object of a given type that contains a value unless uninitialized.  |
| (f) <b>definition</b> _____     | (6) The specification of a name with its type in a program.   |
| (g) <b>variable</b> _____       | (7) Some memory that holds a value of a given type.   |
| (h) <b>function</b> _____       | (8) A conversion of types that may put a value into an object that is too small to hold it.                             |
| (i) <b>type</b> _____           | (9) The basic unit of addressing in most computers.   |
| (j) <b>object</b> _____         | (10) Errors found by the programmer looking for the causes of erroneous results.  |
| (k) <b>bit</b> _____            | (11) Something that must be always true at a given point (or points) of a program.                                      |
| (l) <b>logic errors</b> _____   | (12) Syntax or type errors.   |

2. If  $x$  contains the value 3 before the following instruction is executed

```
for(int i = 0; i < 4; i+=2)
    x *= 5;
```

- What is the value of  $x$  after the loop runs?
- Rewrite the loop as an equivalent **while** loop.
- Rewrite the loop as an equivalent **do-while** loop.

3. Write 216

- in base 2 form. That is, determine binary digits  $a_7, a_6, \dots, a_0$  such that  $a_7 \cdot 2^7 + a_6 \cdot 2^6 + \dots + a_0 \cdot 2^0 = 216$
- in base 16 form. That is, determine hexadecimal digits  $a_1, a_0$  such that  $a_1 \cdot 16 + a_0 = 216$

4. Suppose we declare a variable like so:

```
string place = "BED";
```

- How many bytes of memory would the variable `place` require in memory? Assume that the string is appended by the `'\0'`, or “NULL” character, which takes one byte of all 0 bits.
- How is `place` represented as a sequence of bits in memory? *Hint*: the ASCII code for `'A'` is 65.

5. Suppose you have a point on a plane represented by the variables `ptX` and `ptY` (its  $x$  and  $y$  coordinates). Suppose you also have a rectangle, whose upper left corner is represented by the variables `left` and `top`, and whose bottom right corner is represented by the variables `right` and `bot`. What conditional statement would you write to determine whether or not `(ptX,ptY)` is inside the rectangle or not? That is how would you fill in the condition in the statement below:

```
if(/* fill in condition here */)
    cout << "\nThe point (" << ptX << ", " << ptY << ") is inside the rectangle.";
else
    cout << "\nThe point (" << ptX << ", " << ptY << ") is not inside the rectangle.";
```

6. Consider the following program:

```
1 int main()
  {
3   vector<int> a{3,2,6,1}, b;
   printVector(a);
5   b = bubbleSort(a);
   printVector(b);
7 }

9 vector<int> bubbleSort(vector<int> a)
  {
11  int temp;
   for (int k = 0; k < a.size(); k++)
13  {
       for (int i = 0; i < a.size()-1; i++)
15  {
           if (a[i] > a[i+1])
17  {
               temp = a[i];
               a[i] = a[i + 1];
               a[i + 1] = temp;
21  }
       }
23  }
  }

25 void printVector(vector<int> a)
27 {
   for (int i=0; i <a.size(); i++)
29     cout<<a[i]<<"␣";
   cout<<endl;
31 }
```

- What prototypes should be declared before `main()` ?
- What is the return type of `bubbleSort()` ?
- What is the value of `a.size()` ?
- What is `temp` used for in `bubbleSort()` ?
- Tabulate values of `k`, `i`, `a[i] > a[i+1]` (true or false) and `a` (list the entire vector at each iteration) as the body of `bubbleSort()` is executed.
- There is an error in `bubbleSort()`. How can you fix it? *Hint*: what happens on line 5?

7. (a) Write a C++ program to implement the pseudocode:

```
Set den to one
Get num from user
Set term = num/den (a floating point value)
Set i = 1
set sum = 1
While i less than or equal to three
    i is increased by 1
    term is multiplied by num
    den is multiplied by i
    term is divided by den
    term is added to sum
Print sum
```

- (b) Tabulate values of `i` and values of `term`, `den` and `sum` as the loop is executed if the user enters 2:

i	term	den	sum
1			

8. Write a function that takes a positive integer and determines whether or not it is divisible by some square number,  $k^2 > 1$ . That is,  
**precondition:** A positive integer.  
**postcondition:** `true` if there is some integer  $k > 1$  such that  $n$  modulo  $k^2$  is zero, otherwise, `false`

9. Consider the code below, and assume all the needed libraries are included and using namespace std;

```

1  const int maxint = 25;
   void print(vector<bool> v);
3
   int main() {
5     vector<bool> primes(maxint);
     for(int i = 2; i < maxint; ++i)
7         primes[i] = 1;
     for(int i = 2; i < sqrt(maxint); ++i) {
9         for(int j = 2; j <= maxint/i; ++j)
             primes[j*i] = 0; // multiples of i are composite
11    }
     print(primes);
13 }
   void print(vector<bool> v) {
15     int j = 0;
     for(int i = 0; i < v.size(); ++i) {
17         if(v[i]) {
             cout << i << '\t';
19             if((j+1)%10==0) cout << endl;
             ++j;
21         }
     }
23 }

```

- (a) Describe what the declaration on line 5 does.
- (b) Describe in detail what the loop on lines 6,7 does.
- (c) Complete the table below which threads the values of quantities as the loop on lines 8-11 is executed:

i	j	i*j	primes[i*j]	maxint/i
2	2	4	0	12
	3	6	0	
	4	8	0	
	5	10	0	
	6	12	0	
	7	14	0	
	8	16	0	
	10	20	0	
	12	24	0	
3	2	6	0	8
⋮	⋮	⋮	⋮	⋮

- (d) Why is this code for computing prime numbers not as efficient as it could be? What could you do to improve the efficiency?
- (e) Describe the logic of how the print() function works.